

Math 446 — Final Exam — Review Topics after Exam 2

Chapter 9. Choice's Consequences, continued.

cardinal minimum and supremum lemmas

König's Theorem

cofinality of cardinal numbers

$\kappa < cf(2^\kappa)$

Exercises x9.9, 9.14, 9.20

Chapter 11. Replacement and Other Axioms.

axiom of replacement

transitive sets and the transitive closure

pure sets, grounded sets, axioms of purity and foundation

You are not responsible for the results about graphs, Zermelo universes

Exercises x11.3, 11.5, 11.14

Chapter 12. Ordinal Numbers.

definition and properties of the “von Neumann” map, referred to as o_U
in class

ordinals and the class ON of ordinals

properties and characterization of ordinal numbers

ordinal comparability and the well-ordering of ON

ordinal induction and recursion

+ and \cdot on ordinals

definition and properties of the “von Neumann” cardinals

the sequence of alephs

cardinal arithmetic

cumulative, or rank, hierarchy V_α and the rank of a set

normal operations

cofinality of ordinals and its equivalence with the earlier definition on
cardinals

Exercises x12.5, 12.9, 12.10, 12.13, 12.29