

Name _____ KEY _____

Section 0251

Answer all problems. There are 10 possible points.

1. (6pts) Find the derivative of the following functions (Show all work to receive full credit!):

a) $f(x) = \frac{6}{\sqrt[4]{x}}$

$$f'(x) = \frac{-6}{4} x^{(-1-1)} = -\frac{3}{2} x^{\left(\frac{-1-4}{4}\right)} = -\frac{3}{2} x^{-\frac{5}{4}}.$$

b) $g(x) = \frac{x^4 - 2x + 1}{x}$

$$g(x) = \frac{x^4}{x} - \frac{2x}{x} + \frac{1}{x} = x^3 - 2 + x^{-1}.$$

$$g'(x) = 3x^2 - x^{-2}.$$

2. (4pts) Find all the values of x where the tangent line of the function

$$f(x) = 2x^3 - 9x^2 - 24x + 6 \text{ is horizontal (Show all work to receive full credit!):}$$

The tangent line is horizontal if $f'(x) = 0$.

$$\text{Therefore, } 0 = f'(x) = 6x^2 - 18x - 24 = 6(x^2 - 3x - 4) = 6(x+1)(x-4).$$

Then $x = -1, 4$.