

- Suppose $P(x) : x \in [-1, 2]$ and $Q(x) : x^2 \leq 2$ over the domain $S = [-2, 2]$.
- For which values in the domain is the biconditional $P(x) \leftrightarrow Q(x)$ a true statement?
Note: This is the final question from yesterday's groupwork.
- Suppose $P(x, y) : x^2 - y^2 = 0$ and $Q(x, y) : x = y$. Determine the truth value of $P(x, y) \leftrightarrow Q(x, y)$ for $(x, y) \in \{(1, -1), (3, 4), (5, 5)\}$.

- For statements P and Q show that $(P \wedge (P \rightarrow Q)) \rightarrow Q$ is a tautology by writing out the truth table.

P	Q	$P \rightarrow Q$	$(P \wedge (P \rightarrow Q))$	$(P \wedge (P \rightarrow Q)) \rightarrow Q$
T	T			
T	F			
F	F			
F	T			

- Show that $P \rightarrow (Q \vee R) \equiv (\sim Q) \rightarrow ((\sim P) \vee R)$ by logically manipulating both sides to achieve the same statement.

- Determine with justification if the following are true or false:

(a) $\forall n \in \mathbb{Z}, (2n - 1)/5 \in \mathbb{Z}$.

(b) $\exists n \in \mathbb{Z}, (2n - 1)/5 \in \mathbb{Z}$.

(c) $\exists x \in \mathbb{Z}, \exists y \in \mathbb{R}, x^2 + y^2 = 3$

(d) $\sim (\exists s \in \{3, 5, 11\}, \exists t \in \{3, 5, 11\}, st - 2 \text{ is not prime})$