

Math 140, Jeffrey Adams
Test III, November 6, 1998

IMPORTANT INSTRUCTIONS

1. Write your name, section number, and TA's name on each answer sheet.
 2. Number the sheets 1-4. Do all of the work for problem 1 on sheet 1. You may use the back if necessary – write “*see back of sheet*”. Similarly for problems 2-4.
 3. For full credit you must **show your work**.
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Question 1. (30 points)

(a) Let $f(x) = x^3 - 6x^2 + 9x - 1$. Find the maximum value and minimum value of f on the interval $[0, 2]$.

(b) Let $g(x) = \frac{x^2 + x + 1}{x^3 - x}$. Find all vertical asymptotes and horizontal asymptotes of g .

(c) Find a function $h(x)$ such that $h(0) = 0$ and $h'(x) = e^{-x}$.

Question 2. (30 points)

Let $f(x) = \frac{1+x}{1-x}$, and note that $f'(x) = \frac{2}{(1-x)^2}$ and $f''(x) = \frac{4}{(1-x)^3}$.

- (a) Find all x and y intercepts of f .
- (b) Find all relative maximum values and relative minimum values of f .
- (c) Determine where the graph of f is concave upward and where it is concave downward.
- (d) Find all inflection points of f .
- (e) Find all horizontal asymptotes and vertical asymptotes of f .
- (f) Sketch the graph of f , and include all pertinent labels on the graph.

Question 3. (20 points)

An isosceles triangle has base 4 and height 10. Find the maximum possible area of a rectangle that can be placed inside the triangle with one side on the base of the triangle.

Question 4. (20 points)

(a) Let $f(x) = x^{\frac{7}{3}}$. Find a point c such that $f'(c) = f''(c) = 0$. Show that f does *not* have a relative maximum or relative minimum at c .

(b) Suppose $g(x)$ is a function defined for $x \geq 0$, such that $g'(x)$ has the graph given below. Determine the intervals on which the graph of g is concave up, and those on which it is concave down.