Definitions

straight angle: An angle measuring 180°. It forms a straight line.

vertical angles: When two lines intersect, the angles opposite each other.

<u>angle of rotation</u>: an amount of rotation about a fixed point. One full rotation is 360°. Angles surrounding a point sum to 360° because they constitute one full rotation.

<u>angle formed by two rays with common endpoint P</u>: the smallest amount of counterclockwise rotation about P needed to rotate one of the rays to the position of the other ray.

triangle: A closed shape in a plane consisting of three line segments.

congruent angles: two angles that have the same measure

<u>line segment</u>: the part of a line lying between two points on a line.

ray: the part of a line lying on one side of a point on the line.

right angle: equal to 90° acute angle: less than 90° obtuse angle: greater than 90°

*<u>complementary angles</u>—add to 90° *<u>supplementary angles</u>—add to 180°

Perpendicular: two lines that meet to form right angles

<u>Parallel</u>: two lines in a plane that never meet *<u>congruent segments</u>—have the same length

*midpoint—the point on a line segment that divides it into two congruent segments

*segment bisector—a point or line that divides a segment into two congruent segments

*angle bisector—a ray that divides an angle in half, i.e. into two congruent angles right triangle

scalene triangle: has no equal sides equilateral triangle: has three equal sides isosceles triangle: has at least two equal sides

Quadrilateral: a closed shape in a plane consisting of four line segments

Polygon: a closed shape in a plane consisting of a finite number of line segments

vertex: corner point where two sides meet

interior angle: angle at a vertex, inside the polygon

exterior angle: angle at a vertex formed by extending one side and measuring to the

adjacent side.

square: quadrilateral with four equal sides and four right angles

<u>rectangle</u>: quadrilateral with four right angles <u>rhombus</u>: quadrilateral with four equal sides

<u>parallelogram</u>: quadrilateral with both pairs of opposite sides parallel <u>trapezoid</u>: quadrilateral with at least one pair of opposite sides parallel

*<u>kite</u>—a quadrilateral with two non-overlapping pairs of congruent adjacent sides (ex) Diagonal: line segment connecting two non-adjacent vertices (corners) of a polygon

*opposite angles (in a quadrilateral)—angles that do not share a side

<u>Circle</u>: the collection of all the points in a plane that are a certain fixed distance (the "radius") away from a certain fixed point (the "center") in the plane.

Axioms Summary

These first assumptions will be helpful when we want to add or extend a line in a diagram.

- 1. Two points determine a line (i.e., you can only draw one line through two points).
- 2. A line can be extended indefinitely.
- 3. Given the line I and a point P not on I, there is exactly one line through P parallel to I.
- 4. In a plane, exactly one perpendicular can be drawn from a point to a line.
- 5. In a plane, exactly one perpendicular line can be drawn to a point on a line.
- 6. An angle has exactly one bisector.
- 7. A segment has exactly one midpoint.

These additional assumptions will help us complete proofs:

- 8. All right angles are congruent.
- 9. "Substitution" or "Transitive Property": Things which are equal to the same thing are also equal to each other.
- 10. Algebra: We can use the rules of algebra to solve equations (e.g. we can subtract the same amount from both sides of an equation).
- 12. "Reflexive Property": A segment is congruent to itself; an angle is congruent to itself.
- 13. Lines are parallel if and only if corresponding angles are congruent (parallel postulate)
- 14. Lines are parallel if and only if alternate interior (or exterior) angles are congruent.
- 15. Lines are parallel if and only if same-side interior (or exterior) angles add to 180° (i.e., "are supplementary").

^{*}consecutive angles (in a polygon)—angles that share a side

(up to date) Theorems List (we will add to this list!)

- 1. Vertical angles (opposite angles) are congruent.
- 2. The sum of the interior angles in an n-gon is 180(n-2).
- 3. The sum of the exterior angles of a convex polygon is 360°
- 4. If two triangles share AAS, SSS, SAS, or ASA congruence then they are congruent.
- 5. (Base Angles Theorem) Base angles of a triangle/trapezoid are equal if and only if it is isosceles.
- 6. Given a quadrilateral, it is a parallelogram if and only if opposite sides are congruent.
- 7. Given a quadrilateral, it is a parallelogram if and only if opposite angles are congruent.
- 8. Given a quadrilateral, it is a parallelogram if and only if diagonals bisect each other.
- 9. Given a parallelogram, it is a rectangle if and only if diagonals are congruent.
- 10. Given a parallelogram, it is a rhombus if and only if the diagonals are perpendicular bisectors.
- 11. Rectangles and Rhombi are parallelograms.
- 12. A kite is a trapezoid if and only if it is a rhombus.
- 13. (Pythagorean Theorem) A right triangle with legs of length a, b satisfies $a^2+b^2=c^2$ where c is the length of the hypotenuse.