

Sparse and Low Rank Representations: Analytical Method and Industrial Applications

Instructor: Radu Balan , rvbalan@math.umd.edu

When: Tuesdays, Thursdays 12:30pm-1:45pm

Where: CSIC 4122

Office Information: CSIC 4131 , phone: x5-1217

Office Hours: by appointment

Course Topics:

1. Basic Functional Analysis: Hilbert space, projections, closed subspaces, function spaces; orthonormal bases; frames
2. Fourier analysis (series and transforms)
3. Shift-Invariant spaces: band-limited functions; spaces of splines/polynomial functions
4. Approximation Principles: Non-parametric vs. parametric models, linear vs. nonlinear, deterministic vs. stochastic estimation
5. Linear models:
 - 2.1 Stochastic approach: Karhunen-Loev decomposition; PCA; ICA
 - 2.2 Deterministic approach: case studies: spectral approximations; Fix-Strang conditions for shift-invariant spaces; Blind source separation for sparse signals.
6. Model selection:
 - 3.1 Classic principles: Akaike information criterion; Bayesian information criterion; Minimum description length
 - 3.2 Sparse models
7. Nonlinear models
 - 4.1 Matrix completion problem
 - 4.2 Phaseless reconstruction

Recommended Readings: selected list of papers posted on Canvas

Grading Info: Homeworks (25%), exam (25%), project/report (50%)