- 1. Ex. 1, 3, 6, 7, 8, Sec.8.3, Cooper.
- $2. \ Let$

$$f(x) = \frac{1}{1+x^2}.$$

The function f is analytic on $(-\infty, \infty)$. However if we expand f in a power series about any point x_0 , the radius of convergence $R(x_0)$ is finite. Find the formula for $R(x_0)$.

3. Obtain a series expansion for the integral

$$\int_0^{1/2} \frac{1}{1+x^4} \, dx$$

and justify your calculation.